Total electric potential energy, *U*, of a system of charges is obtained from the work done by an external *F*, (*W*\*) to assemble the system, bringing each charge in from ∞. In terms of work done by the field, *W*\*= -*W*.



• Bring  $q_1$  from  $\infty$ ,  $W^* = 0$  since no electric F yet

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## Potential Energy (Fig. 25-16)

Potential due to q<sub>1</sub> is

$$V = k \frac{q_1}{r} \qquad \stackrel{q_1}{\xleftarrow} r \xrightarrow{q_2} f$$

Bring q<sub>2</sub> in from infinity. From definition of potential energy

$$U = -W = W^* = q_2 V = k \frac{q_1 q_2}{r}$$
 or  $U = k \frac{q_1 q_2}{r}$ 

- Charges of like sign,  $W^*$  and U are +
- Charges of opposite sign, W\* and U are -

- What is the potential energy when add an additional charge to system?
- Move q₁ from ∞, W\* = U = 0
  Move q₂ from ∞

$$W_{12}^* = U_{12} = k \frac{q_1 q_2}{d}$$



## Potential Energy (Fig. 25-17)

• Now bring in q<sub>3</sub>

$$W_{13}^* = U_{13} = k \frac{q_1 q_3}{d}$$

Must also remember q<sub>2</sub>

$$W_{23}^* = U_{23} = k \frac{q_2 q_3}{d}$$



 Total potential energy is the scalar sum

$$U = U_{12} + U_{13} + U_{23}$$

$$q_1 = +q, \quad q_2 = -4q, \quad q_3 = +2q$$



$$U = k \left( \frac{(+q)(-4q)}{d} + \frac{(+q)(+2q)}{d} + \frac{(-4q)(+2q)}{d} \right) = -k \frac{10q^2}{d}$$

#### **Electric Potential for Conductors**

Using what we know about conductors

• E = 0 inside

All excess charge is on surface

- All points of a conductor whether inside or on the surface – are at the same potential
  - A conductor is an equipotential

## Electric Potential for Conductors (Fig. 25-18)





# Electric Potential (Checkpoint #3)

- An electron moves along 5 different paths between parallel equipotential surfaces
- a) What is the direction of the *E* associated with the surfaces?



 Positive potentials which decrease going to the right.

## **Electric Potential (Exercise)**

 b) Rank the paths by amount of work we do (greatest first).

$$W^* = -W = q\Delta V$$

$$W^* = q \left( V_f - V_i \right)$$

$$90 V \quad 80 V \quad 70 V \quad 60 V \quad 50 V \quad 40 V$$

Electron gives

$$W^*_{Path-1} = -q(70-80) = +10q$$

3, then 1 & 2 & 5, last 4