Complete Electric Dipole Response and the Neutron Skin in $^{208}$Pb


Research Center for Nuclear Physics, Osaka University, Ibaraki, Osaka 567-0047, Japan
Institut für Kernphysik, Technische Universität Darmstadt, D-64289 Darmstadt, Germany
Department of Physics, Osaka University, Toyonaka, Osaka 560-0043, Japan
Kernfysisch Versneller Instituut, Universiteit van Groningen, Zernikelaan 25, NL-9747 AA Groningen, The Netherlands
Department of Physics and Astronomy, Texas A&M University–Commerce, Commerce, Texas 75429, USA
School of Physics, University of the Witwatersrand, Johannesburg 2050, South Africa
Department of Physics, Kyushu University, Fukuoka 812-8581, Japan
Cyclotron and Radioisotope Center, Tohoku University, Sendai, 980-8578, Japan
Department of Physics, Kyoto University, Kyoto 606-8502, Japan
GSI Helmholtzzentrum für Schwerionenforschung, D-64291 Darmstadt, Germany
Institut für Theoretische Physik, Goethe-Universität, 60438 Frankfurt am Main, Germany
Center for Nuclear Study, University of Tokyo, Bunkyo, Tokyo 113-0033, Japan
Themis LABS, Somerset West 7129, South Africa
ECT*, Villa Tambosi, I-38123, Villazzano (Trento), Italy
Instituto de Física Corpuscular, CSIC-Universidad de Valencia, E-46071 Valencia, Spain
Department of Physics, Niigata University, Niigata 950-2102, Japan
RIKEN Nishina Center, Wako, Saitama 351-0198, Japan
National Institute of Radiological Sciences, Chiba 263-8555, Japan
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A benchmark experiment on $^{208}$Pb shows that polarized proton inelastic scattering at very forward angles including $0^\circ$ is a powerful tool for high-resolution studies of electric dipole (E1) and spin magnetic dipole (M1) modes in nuclei over a broad excitation energy range to test up-to-date nuclear models. The extracted $E1$ polarizability leads to a neutron skin thickness $r_{\text{skin}} = 0.156^{+0.025}_{-0.021}$ fm in $^{208}$Pb derived within a mean-field model [Phys. Rev. C 81, 051303 (2010)], thereby constraining the symmetry energy and its density dependence relevant to the description of neutron stars.

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The electric dipole (E1) response of nuclei is dominated by the giant dipole resonance (GDR), a highly excited collective mode above the particle emission threshold [1]. Its properties are well understood, but recent interest focuses on evidence for a soft mode in neutron-rich nuclei below the GDR which is termed the pygmy dipole resonance (PDR). Because of the saturation of the nuclear density, excess neutrons might form a skin whose oscillations against an isospin-saturated core should give rise to a low-energy E1 mode [2]. Therefore, the PDR may shed light on the formation of neutron skins in nuclei [3]. Another quantity related to nuclear E1 modes is the symmetry energy acting as a restoring force. The E1 strength distribution carries information on its poorly known magnitude and density dependence [4], indispensable ingredients for the modeling of the equilibrium properties of neutron stars [5].

A case of special interest is the doubly magic nucleus $^{208}$Pb. In a measurement of parity-violating elastic electron scattering at JLAB, the PREX Collaboration [6] aimed at the first model-independent determination of the neutron skin thickness in $^{208}$Pb. However, the recent result $r_{\text{skin}} = 0.34^{+0.13}_{-0.11}$ fm suffers still from limited statistics. Studies of energy density functionals (EDFs) [7] using Skyrme forces [8] or a relativistic framework [9] suggest the nuclear dipole polarizability $\alpha_D$ as an alternative observable constraining both neutron skin and symmetry energy. The polarizability is related to the photoabsorption cross section $\sigma_{\text{abs}}$ [10],

$$\alpha_D = \frac{\hbar c}{2\pi^2 e^2} \int \frac{\sigma_{\text{abs}}}{\omega^3} d\omega,$$

where $\omega$ denotes the photon energy. Because of the inverse energy weighting, $\alpha_D$ depends on the $E1$ strength at low energies. Theoretically, advanced methods exist in closed-shell nuclei for a realistic description of the $E1$ strength distributions [11].

The centroid of the PDR lies typically in the vicinity of the neutron emission threshold ($S_n$). Data on the PDR in very neutron-rich nuclei are still scarce [12–14]. Stable
nuclei at different shell closures have been explored with the \((\gamma, \gamma')\) reaction (Ref. [15] and references therein). While this technique provides important information on the fine structure of the PDR, it is essentially limited to excitation energies up to \(S_n\), and unobserved branching ratios of the \(\gamma\) decay to the excited states may require corrections for the total strength [16]. Measurements of decay neutrons are constrained to energies \(E_x > S_n\), and uncertainties in the vicinity of \(S_n\) are large. We present here a new experimental tool, viz., polarized proton scattering at angles close to and including \(0^\circ\), to provide the complete \(E1\) response in nuclei up to excitation energies well above the region of the GDR. At proton energies of \(200–400\) MeV the cross sections at small momentum transfers are dominated by isovector spin-flip \(M1\) transitions (the analog of the Gamow-Teller mode) and by Coulomb excitation of non-spin-flip \(E1\) transitions [17,18]. A separation of these two contributions, necessary for an extraction of the \(E1\) response, is achieved by two independent methods: a multipole decomposition analysis of the angular distributions (MDA) and the measurement of polarization transfer (PT) observables.

The \(^{208}\text{Pb} (\vec{p}, \vec{p'})\) experiment was performed at RCNP, Osaka, Japan. Details of the technique can be found in [19]. In the present work [20], a proton beam of \(295\) MeV with intensities \(2–10\) nA and an average polarization \(P_0 \approx 0.7\) bombarded an isotopically enriched \(^{208}\text{Pb}\) foil with an areal density of \(5.2\) mg/cm\(^2\). Data were taken with the Grand Raiden spectrometer [21] in an angular range \(0^\circ–2.5^\circ\) and for excitation energies \(E_x \approx 5–23\) MeV. Sideway (\(S\)) and longitudinally (\(L\)) polarized proton beams were used to measure the polarization transfer coefficients [22] \(D_{SS'}\) and \(D_{LL'}\), respectively. Additional data with unpolarized protons were taken at angles up to \(10^\circ\). Utilizing dispersion matching techniques, a high energy resolution \(\Delta E \approx 25\) keV (FWHM) could be achieved.

Figure 1(a) displays a spectrum at \(0^\circ\). Strong transitions at low excitation energies, a resonance-like structure close to \(S_n = 7.37\) MeV and the prominent isovector giant dipole resonance, peaked at \(E_x = 13.4\) MeV with pronounced fine structure, are observed. The total spin transfer \(\Sigma\) can be extracted from the measured PT observables which at \(0^\circ\) takes a value of one for spin-flip (\(\Delta S = 1\)) and zero for non-spin-flip (\(\Delta S = 0\)) transitions [23]. Figure 1(b) shows \(\Sigma\) for \(E_x = 5–22\) MeV. Values between 0 and 1 result from a summation over partially unresolved transitions with different spin-flip character. The data reveal a concentration of spin-flip strength in the energy region 7–9 MeV, where the spin-\(M1\) resonance in \(^{208}\text{Pb}\) is located [18], while the bump between 10 and 16 MeV has \(\Delta S = 0\) character consistent with the excitation of the GDR. The \(\Delta S = 1\) strength above the GDR may result from the \(\Delta S\) components of the on-setting quasi-free scattering cross section [24].

A multipole decomposition was performed for angular distributions of the cross sections in the PDR and GDR regions. Theoretical angular distributions were calculated with the code \textsc{dwba}07 [25] using microscopic quasiparticle-phonon model (QPM) wave functions [26] and the Love-Franey effective proton-nucleus interaction [27]. The interference of Coulomb and nuclear contributions to the cross sections was taken into account for \(E1\) transitions. For a satisfactory description of the data it was sufficient to include, besides \(E1\) and \(M1\), one higher multipole representative for all other contributions. The latter was chosen to be either \(E2\) or \(E3\) in the region of the PDR. In the GDR region the \(M1\) contribution was zero within error bars and was replaced by a phenomenological background describing the data at high excitation energies. The weight of each component was determined by a least-squares fit to the data.

FIG. 1 (color online). (a) Spectrum of the \(^{208}\text{Pb} (\vec{p}, \vec{p'})\) reaction at \(E_p = 295\) MeV with the spectrometer placed at \(0^\circ\). (b) Total spin transfer \(\Sigma\).
Cross sections for $\Delta S = 0$ and 1 from the MDA and PT analysis for $E_x < 9$ MeV are compared in Fig. 2. Within uncertainties the correspondence between the two completely independent decomposition methods is excellent. This puts confidence in the MDA results discussed in the following, which provide much better resolution because of the superior statistics compared to a double scattering measurement of PT. In the GDR region no direct comparison is possible because of the unknown $\Delta S$ content of the phenomenological background. However, both methods agree that $\Delta S = 1$ contributions are very small.

Next we show that reliable $B(E1)$ strengths can be extracted from the $(p, p')$ data. While the angular dependence of $E1$ transitions is generally state dependent because of the Coulomb-nuclear interference, cross sections at very small angles ($\Theta_{lab} < 1^\circ$) arise purely from Coulomb excitation. Thus the conversion from cross section to strength is straightforward using semiclassical theory [28]. The $B(E1)$ distribution up to 8.2 MeV is compared in Fig. 3(a) with an average over all available $^{208}$Pb($\gamma, \gamma'$) and $^{207}$Pb($n, \gamma$) data (Refs. [26,29–31] and references therein). Excellent agreement is obtained up to $S_n$. The excess strength in the $(p, p')$ data above the neutron threshold can be attributed to previously unknown neutron decay widths of the excited $1^-$ states, which modify the branching ratios in the $\gamma$-decay experiments and thus the extracted $B(E1)$ values. Figure 3(b) shows the photoabsorption cross sections in the GDR region together with results from a $(\gamma, x\gamma)$ [32] and a total photoabsorption [33] experiment. Again, very satisfactory agreement of all three measurements is observed.

Figure 4(a) displays the experimental $B(E1)$ distribution. From the numerous computations of the $E1$ response in $^{208}$Pb we show in Fig. 4(b) recent results from the QPM [26], and in Fig. 4(c) the relativistic time-blocking approximation (RTBA) [34]. The QPM calculations contain up to 3-phonon configurations for $E_x \leq 8.2$ MeV and 2-phonon configurations in the GDR region. Although the RTBA has recently been extended to include the full set of 2-phonon states [35], the results shown are based on a particle-hole phonon model space [34]. In the low-energy region, the QPM provides a realistic description of the fragmentation, but the overall strength is somewhat too small, while the RTBA model space is not yet sufficient to reproduce the fine structure, and the strength is somewhat too large. The width of the GDR is roughly reproduced by both models. Within the QPM the effective isovector interaction strength is adjusted to the experimental GDR centroid at 13.4 MeV. The RTBA calculations are fully self-consistent and the GDR centroid determined by the covariant EDF parametrization amounts to 12.9 MeV for the NL3 parameter set used [36]. Such a comparison between high-precision data and the 3-phonon version of the QPM guides the next generation of self-consistent extensions of the covariant EDF. Taking into account higher-order configurations, ground state correlations, and pairing vibrations should improve agreement with the data.

Finally, as discussed above, an important quantity is the electric dipole polarizability. We find $\alpha_D = 18.9(13)$ fm$^3/e^2$ for the $E1$ strength up to 20 MeV. By taking an average of all available data including excitation

![Figure 3](color online). (a) $B(E1)$ strengths in $^{208}$Pb in the region $E_x \approx 4.8–8.2$ MeV as deduced from the present work in comparison with $(\gamma, \gamma')$ and $(n, \gamma)$ experiments [26,29–31]. (b) Photoabsorption cross sections in the GDR region from the present work compared to $(\gamma, x\gamma)$ [32] and total photoabsorption [33] measurements.

![Figure 4](Experimental $B(E1)$ strength distribution in (a) $^{208}$Pb in comparison to (b) QPM and (c) RTBA calculations described in the text. Note the different scales below and above 8.2 MeV.)
energies up to 130 MeV [32,33], a result with further reduced uncertainty $\alpha_D = 20.1(6) \text{ fm}^3/e^2$ is obtained. The covariance ellipsoid of the correlation between $\alpha_D$ and the neutron skin thickness $r_{\text{skin}}$ in the approach of Ref. [8] is shown in Fig. 5. Only with the present precision for $\alpha_D$ (hatched band) one can constrain the neutron skin thickness to $r_{\text{skin}} = 0.156^{+0.025 \pm 0.021} \text{ fm}$. The lighest most precise determinations of this quantity for $^{208}\text{Pb}$ [37,38] deduced from exotic atoms ($r_{\text{skin}} = 0.18 \pm 0.02 \text{ fm}$) and hadron scattering ($r_{\text{skin}} = 0.211^{+0.054 \pm 0.063} \text{ fm}$), respectively, are in excellent agreement with our result based on a totally independent method. Recent calculations of neutron matter and neutron star properties [39] in the framework of chiral effective field theory suggest $r_{\text{skin}} = 0.17 \pm 0.03 \text{ fm}$. The predictions are sensitive to three-nucleon forces, which may be further constrained by the present results. Since the correlation between polarizability, neutron skin thickness, and symmetry energy is model dependent, viz., $r_{\text{skin}} \propto \alpha_D \cdot a_{\text{sym}}$ [40], a systematic study with a variety of EDFs as well as experimental tests in other nuclei would be important.

To summarize, polarized proton scattering at very forward angles is a tool to study, with high resolution, the complete electric dipole response of nuclei from low excitation energies up to the GDR. The $E1$ strength distribution deduced in a benchmark experiment on $^{208}\text{Pb}$ is in excellent agreement with available data. It provides, however, new information in the region around the neutron emission threshold where all previous experiments had limited accuracy. A precise value for the $E1$ polarizability can be extracted with important consequences for a determination of the neutron skin and the symmetry energy in neutron-rich nuclei. Although controversially discussed [8], $r_{\text{skin}}$ may independently be derived from a similar correlation with the PDR strength [9,13], which is accurately determined by the present data as well. Beyond these results, the experiment also confirms the spin-M1 resonance in $^{208}\text{Pb}$. Furthermore, the fine structure of the dipole modes contains information on level densities [41] and characteristic scales [42], giving insight into their dominant damping mechanisms.

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FIG. 5 (color online). Extraction of the neutron skin in $^{208}\text{Pb}$ based on the correlation between $r_{\text{skin}}$ and the dipole polarizability $\alpha_D$ established in Ref. [8].

\[ r_{\text{skin}} = 0.156^{+0.025 \pm 0.021} \text{ fm} \]

\[ \alpha_D = 20.1(6) \text{ fm}^3/e^2 \]


