Fusion11 Conference Summary

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Abstract. A summary account of the conference "Fusion11", held in Saint Malo, France, May 2-6, 2011.

1 Introduction

Navin Alahari (Chair) made a short overview of what the community expects to learn, what are the main experimental and theoretical difficulties, and how we can proceed in the future. In particular, he pointed out that he organized this meeting because "there are some questions that cannot be answered with Google". Reluctantly, I tend to agree.

There were 77 talks by experts in the field. I will comment on a few of the physics topics discussed during the presentations. My description is evidently limited in scope due to the short space.

2 New facilities

Sidney Gales presented an overview of the future of the SPIRAL 2 facility at GANIL, France, which promises to break the high intensity frontier for both stable and "*exotic*" beams. The construction will occur in two phases, with the production of radioactive beams planned for 2015. Physics with radioactive and stable-ion high-intensity beams at 1-20 MeV/nucleon will allow, among many other processes, the study of fusion-evaporation with very small cross sections, possibly at the nb level.

Peter Thirolf introduced the Extreme Light Infrastructure (ELI-Nuclear Physics) facility to be built in Bucharest, Romania, by the European Community. This facility will be devoted to research with high-intensity lasers (20 petawatts), up to 5 orders of magnitude higher than today's laser intensity. It would eventually allow to study laser induced fission-fusion events. If all goes as planned, the facility would be operational by 2015.

P. Monier-Garbet also described the outcome of a new heavy-weight facility: ITER, the *international project for thermonuclear fusion*. This project (presently estimated at 15 billion euros) will open a new epoch for studies of fusion plasmas. ITER is designed to confine a deuteron-tritium plasma in which α -particle heating dominates all other forms

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of plasma heating. ITER's principal goal is to design, construct and operate a tokamak experiment at a scale which satisfies the objective of using *fusion energy for peaceful purposes*. ITER's basic research will be atomic physics and material science. The generation of commercial energy by using thermonuclear fusion will be a quest for future post-ITER projects. Humanity will profit enormously if this is realized.

3 Fusion Cross Sections

As mentioned by *S. Umar*, no practical ab-initio manybody theory for fusion exists. All approaches involve two prongs: a) Calculate an ion-ion (usually one-dimensional) phenomenological potential (Wood-Saxon, proximity, folding, Bass, etc.) using frozen densities, or microscopic, macroscopic-microscopic methods using collective variables (CHF, ATDHF, empirical methods), and b) Employ quantum mechanical tunneling methods for the reduced onebody problem (WKB, IWBC), incorporating quantum mechanical processes by hand, including neutron transfer and excitations of the entrance channel nuclei (CC).

3.1 Barrier Penetration Model (BPM)

Fusion cross sections can be calculated from the equation

$$\sigma_F(E) = \pi \bar{\lambda}^2 \sum_{\ell} (2\ell + 1) P_{\ell}(E), \qquad (1)$$

where *E* is the center of mass energy, $\overline{\lambda} = \sqrt{\hbar^2/2mE}$ is the reduced wavelength and $\ell = 0, 1, 2, \cdots$. The cross section is proportional to $\pi \overline{\lambda}^2$, the area of the quantum wave. Each part of the wave corresponds to different impact parameters having different probabilities for fusion. As the impact parameter increases, so does the angular momentum, hence the reason for the $2\ell + 1$ term. $P_{\ell}(E)$ is the probability that fusion occurs at a given impact parameter, or angular momentum. The barrier penetration method (BPM) assumes that fusion occurs when the particle (with

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Fig. 1. Fusion cross section of $^{64}+^{64}$ Ni as a function of the center of mass energy [4]. The dashed (solid) curve is a BPM (coupled-channel) calculation (Courtesy of *C.L. Jiang*).

mass *m*) penetrates the Coulomb barrier and P_{ℓ} is calculated in a one-dimensional potential model, e.g. by using the WKB approximation or alike.

From $\sigma_{\ell} = \pi \bar{\lambda}^2 (2\ell + 1) P_{\ell}$ one can calculate the average value of ℓ from $\langle \ell(E) \rangle = \sum_{\ell} \ell \sigma_{\ell} / \sum \sigma_{\ell}$ and many other relevant quantities. Sometimes, for a better visualization, or for extrapolation to low energies, one uses the concept of *astrophysical S-factor*, redefining the cross section as

$$\sigma_F(E) = \frac{1}{E} S(E) \exp\left[-2\pi\eta(E)\right],\tag{2}$$

where $\eta(E) = Z_1 Z_2 e^2/\hbar v$, with v being the relative velocity. The exponential function is an approximation to $P_0(E)$ for a square-well nuclear potential plus Coulomb potential, whereas the factor 1/E is proportional to the area appearing in Eq. 1. Sometimes one just plots the cross section as $L(E) = \ln[E\sigma_F(E)]$.

3.2 Optical Potentials (OP)

In order to use Eq. 1 one needs the nucleus-nucleus potential. This is a *badly known beast*. In some cases, one includes the effects of other relevant non-fusion channels (which might be a very large number, say ∞). Then one adds an imaginary part to the real potential and it becomes much more than a beast; something like a combination of the *Devil*[©], *the Alien*[©] and *the Predator*[©]. Some have tried to tame this thing from first principles. But, except for few heroic attempts, we seem to have given up. We just fit whatever we can fit and we get whatever parameters of a potential function we can. Then we wisely call it the "OP".

In this meeting there were some discussions on the OP appropriate for fusion reactions. *D. Pereira* reported extensions of the São Paulo potential, and a new approach for its imaginary part to account for surface dissipative



Fig. 2. Schematic representation of CDCC transitions. (Courtesy of *F. Canto*).

processes in heavy ion reactions. *Pereira* showed that this method could reproduce the ⁷Li(25 MeV)+¹²⁰Sn and the ⁴He(230 MeV)+¹²C elastic scattering data rather well. The *São Paulo potential* has become popular in fusion reactions, due to its simple form [1]. So, does the M3Y potential, which was originally developed to treat heavy ion collisions at $E \sim 100$ MeV/nucleon. It does not really matter: *we love delta-function* potentials. In fact, looking from very far away, the nucleon-nucleon potential does indeed resembles a delta-function. An that is why we use them in effective field theories, mean field calculations (Skyrrme interaction), and in many other areas. Simple.

G. Marti presented results for ^{8,7}Li +²⁰Se elastic scattering at low energies. The data seem to show another effect which goes by the name "*threshold anomaly*". This was also discussed in the talk by *M. Sinha*. After fitting the OP to elastic scattering data, the anomaly appears in plots of energy dependence of the real, *V*, and imaginary, *W*, separate parts of the OP at a certain nucleus-nucleus distance. As the bombarding energy decreases, *W* remains rather flat and below a certain energy value it quickly drops to zero, whereas *V* increases slowly and below the same energy reverses its trend [2]. The behavior of *V* and *W* is compatible with dispersion relations (Yes. We believe that the *OP is an analytic function* in a complex plane!).

Fusion with loosely bound nuclei shows a "breakup threshold anomaly", meaning a small rise of the potentials before the anomaly threshold [3]. I am not sure what kind of physics one wants to extract from (breakup) threshold anomalies. The physics seems to be non-universal, e.g., *Marti* claims that, for the elastic scattering of ⁷Li the behavior of both types of potentials as a function of energy is compatible with the presence of the threshold anomaly. But *C.S. Palshetkar* has reported the absence of the anomaly for ⁹Be+⁸⁹Y system. Do you want to know what anomaly means? "Look! I have found something new!".

C.J. Lin also explored the concept of "*surface anomaly*". What is anomalous here? The diffuseness parameters *a* of



Fig. 3. Barrier distribution function from ²⁰Ne+^{58,60,61}Ni quasielastic scattering measurements (Courtesy of *A. Trczcińska*).

interaction potentials extracted from the fusion data at not only high energies but also extremely low energies are prominent larger than the traditional value (0.65 fm).

S. Umar discussed results from Time-Dependent Hartree-Fock (TDHF) calculations using Skyrme functionals. His goal was to deduce microscopically the potential barriers needed to calculate fusion reaction cross sections. Although heavy systems pose a greater challenge, such microscopic calculations may provide an insight into these collisions.

3.3 Channel Coupling (CC)

It is well know that the BPM does not work. A good example is shown in figure 2, taken from Ref. [4]. Only by including coupling to other channels, the fusion cross sections can be reproduced. In fact, sub-barrier fusion enhancement can be easily understood. Assume that the initial channel energy *E* splits into two channel energies during fusion, $E_1 = E + \Delta$ and $E_2 = E - \Delta$. Then the cross section becomes an approximate energy average of the BPM, $\sigma_F(E) \sim [\sigma_F(E_1) + \sigma_F(E_2)]/2$. Due to the exponential behavior of tunneling probabilities, the decreased cross section $\sigma_F(E_1) < \sigma_F(E)$ more than compensates the increase $\sigma_F(E_2) > \sigma_F(E)$ due to the reduction of the barrier height.

In coupled channels schemes one expands the total wavefunction for the system as

$$\Psi = \sum_{i,k} a_i(\alpha, q_k) \phi(\alpha, q_k), \tag{3}$$

where ϕ form the channel basis, α is a dynamical variable (e.g., the distance between the nuclei), and q_k are intrinsic coordinates. Inserting this expansion in the Schrödinger equation yields a set of CC equations in the form

$$\frac{da_k}{d\alpha} = \sum_j a_j \langle \phi_k | U | \phi_j \rangle \, e^{iE_a \alpha},\tag{4}$$

where U is whatever potential couples the channels k and j and $E_{\alpha} = E_{\alpha}^{(k)} - E_{\alpha}^{(j)}$ is some sort of transition energy, or transition momentum. In the presence of continuum states, continuum-continuum coupling(relevant for breakup channels) can be included by *discretizing the continuum*. This goes by the name of Continuum Discretized Coupled-Channels (CDCC) calculations. Fancy, but also vulgar. There are several variations of CC equations, e.g., a set of differential equations for the wavefunctions, instead of using basis amplitudes.

Coupled channels calculations were discussed in details by *L.F. Canto* in his review talk of fusion reactions. CDCC calculations for d+A with rotational and vibrational channels was reported by *P. ChauHuu-Tai*, while *A. Moro* discussed a simultaneous analysis of elastic, breakup, and fusion channels for the ⁶He+²⁰⁸Pb reaction at energies near the Coulomb barrier. It seems that continuum-continuum couplings hinder fusion, specially above the barrier, but the reason is not well understood.

Coupled channels calculations with a large number of channels in continuum couplings, is one of the least controllable calculations in physics. Anything can happen because of the phases of matrix elements: the couplings can add as +-+--++ (destructive) or as +++-++++ or as ---+--- (constructive), depending on the system and on the nuclear model. Such suppressions or enhancements are difficult to understand. It is simply disgusting. Maybe we should not try to understand. But as Wigner once said: "it is nice that your computer can understand this stuff. But I wish I could understand it myself".

CDCC calculations were also reported by *K. Hagino* for ¹⁶O+²⁰⁸Pb. He included collective and non-collective states, weakly coupled, a total of 64 non-collective levels up to 7 MeV, with a nearly "complete" level scheme both for the excitation energies E^* as for the β_{λ} parameters of a deformed nuclear model. He concluded that the energy dependence of fusion cross section is not altered much by these couplings.

Coupled channels calculations were also reported by *T*. *Ichikawa*. *C.J. Lin* also claimed that the "surface anomaly" (see section 3.2) disappears when CC are taken into account.

3.4 Barrier Distribution

One can try to extract some extra juice from a set of experimental data by recasting them in a different way. For example, assume an extreme classical model in which fusion occurs. Also assume that fusion is hindered by Coulomb recoil. Then the fusion cross section is given approximately by $\sigma_F \sim (1 - V_B/E)\Theta(E - V_B)$ where $\Theta(x) = 0$ for $x \le 0$, and $\Theta = 1$, otherwise. $V_B = Z_1 Z_2 e^2/R$ is the Coulomb barrier height and R is the touching distance between the nuclei. In this approximation, the second derivative of σ_F yields

$$\frac{d^2\sigma_F}{dE^2}\sim \delta(E-V_B),$$

i.e. it spikes at the value of the Coulomb barrier height. Quantum mechanics smears out the δ -function [5], but



Fig. 4. *S*-factors for ²⁸Si+³⁰Si, ²⁷Al+⁴⁵Sc and ²⁸Si+⁶⁴Ni. (Courtesy of *C.L. Jiang*).

 $d^2\sigma_F/dE^2$ should still peak at the position of the Coulomb barrier height. Coupling to other channels fragments the peak and broadens it further, as seen in experiments. $d^2\sigma_F/dE^2$ is thus a probe of *barrier heights* [6].

Quasi-elastic scattering maybe defined as a sum of all reaction processes other than fusion, e.g. elastic scattering, inelastic scattering, transfer, breakup, and so on. Thus fusion and quasi-elastic (qe) scattering are complementary to each other: if $d^2\sigma_F/dE^2 \sim \delta(E-V_B)$, a similar relationship should be applicable to σ_{qe} . It turns out that this is true for the ratio of σ_{qe} and $\sigma_{Ruth}(E)$. This reasoning leads to

$$\frac{d}{dE} \left[\frac{\sigma_{qe}(E)}{\sigma_{Ruth}(E)} \right] \sim \delta(E - V_B).$$
(5)

The advantage of using $D_{eq} = -d[\sigma_{qe}/\sigma_{Ruth}]/dE$ over $d^2\sigma_F/dE^2$ is that less data accuracy is required: a first derivative is much easier to do. σ_{qe} is also a sum of everything: a very simple charged-particle detector can measure it [7]. Measuring σ_F requires a specialized recoil separator to separate evaporation residues (ER) from the incident beam: ER and fission for heavy systems.

Data for barrier distribution were presented by *G*. Montagnoli for ⁴⁰Ca+⁴⁰Ca, by *C.J. Lin* for ^{6,7}Li+²⁰⁸Pb, ²⁰⁹Bi and by *A. Trczcińska* for ²⁰Ne+^{58,60,61}Ni (see figure 3). Remarkable agreement between $d[\sigma_{qe}/\sigma_R]/dE$ and $d^2\sigma_F/dE^2$ is seen in most data. Montagnoli infers from her data that below the barrier, the log slope of the excitation function for ⁴⁰Ca+⁴⁰Ca has a small plateau and starts again increasing at lower energies. *A. Trczcińska* concludes that for ⁵⁸Ni the distribution has a clearly visible "structure" (figure 3), whereas for heavier Ni isotopes the structure is smoothed out (for ⁶⁰Ni partly, for ⁶¹Ni completely).

3.5 Fusion Hindrance

In figure 2 one notices that CC calculations do not quite reproduce the data, specially at deep sub-barrier energies. Our colleagues are working hard to gather data and understand this phenomenon. Cross sections need to be measured at very low energies, a real challenge for accelerator and detector development. As for theorists, there seems to



Fig. 5. Importance of deformation and orientation on the relative nucleus-nucleus potential. (Courtesy of *B. Yilmaz*).

be two main streams of thought. Well, just one: do everything as usual, but modify what happens when nuclei come very close, below the touching distance. A popular story goes like this: build a potential from the M3Y interaction (there is a huge *M3Y fan-club* out there). Then claim that Pauli principle (quoting *C. Simenel: if you do not know what to ask, ask me about the Pauli principle*) modifies the interior of the potential, decreasing its depth. This solves something, as M3Y yields a too deep central part of the potential. In Ref. [8] it was also shown that this procedure also reproduces the nuclear incompressibility and the fusion hindrance in ¹⁶O+²⁰⁸Pb deep sub-barrier fusion.

In Ref. [9] the way to explain fusion hindrance was to assume a neck formation and the onset of damping for distances smaller than the touching radius. In summary, below the touching distance, something weird (*damping is a sort of physics hidden under a knob*) happens, leading to fusion hindrance.

C.L. Jiang claims that all Q < 0 fusion systems must have an *S* factor maximum, because S(E) = 0, when E = -Q. Makes sense. This is shown in the rightmost panel of figure 4. As for Q > 0 (most reactions in stars occur in this way) there is no such requirement. Usually the Sfactors remain finite at E = 0. But as shown in the two left panels of figure 4, this is not really the case: a proof that fusion hindrance also occur for Q > 0 fusion reactions. Intriguing. He also reported a first evidence of an S factor maximum in the positive Q-value system ${}^{40}\text{Ca}{}^{+48}\text{Ca}$. But no firm conclusion can be made about the nature of the *S* factor maximum, which is limited by background levels. *A. Shrivastava* reported that no hindrance was observed in the fusion of ${}^{7}\text{Li}({}^{12}\text{C}){}^{+197}\text{Pt}$.

G.G. Adamian discussed theoretical methods to calculate sub-barrier capture using the *quantum diffusion approach*. This method takes into account the fluctuation and dissipation effects in collisions which model the coupling of the relative motion with various channels. He claims that the effect of the change of fall rate of sub-barrier capture cross section should be in the data if we assume that the friction starts to act only when the colliding nuclei approach the barrier. But at extreme sub-barrier energies the



Fig. 6. Transfer probabilities for multineutron transfer in 96 Zr+ 40 Ca. (Courtesy of *L. Corradi*).

experimental data still have large uncertainties to make a firm experimental conclusion about this effect [11].

B. Yilmaz claimed that a classical treatment of the relative motion is a good approximation at near-barrier energies. Also, the quantal effects of the surface modes cannot be neglected. But it is possible to include them within a semi-classical approximation. In this model, the force on the nuclei follow the equation

$$\frac{dP}{dt} = -\frac{dV_C(R)}{dR} - \frac{dV_N(R, \Omega, \alpha_\lambda)}{dR} + \frac{\ell(\ell+1)\hbar^2}{\mu R^3} - \beta(R)P + F(t),$$
(6)

where Ω is the nuclear orientation, β is a friction coefficient and *F* is a fluctuating force satisfying $\langle F(t) \rangle = 0$ and $\langle F(t)F(t) \rangle = 2\mu\beta kT\delta(t - t')$, where the temperature *T* is defined by the excitation energy. Quantum fluctuations are allowed through the coupling to surface mode amplitudes α_{λ} . Yilmaz showed the importance of deformation and orientation on the relative nucleus-nucleus potential, seen in figure 5. This model is also able to explain fusion hindrance.

G.Montagnoli reported that ⁴⁸Ca+⁴⁸Ca new data are nicely reproduced with CC calculations using a shallow ion-ion potential, à la Ref. [8]. K. Washiyama discussed a beyond mean-field approach to heavy-ion reactions around the Coulomb barrier with a stochastic description of energy dissipation. He obtains a dynamical reduction in the nucleus-nucleus potential, in good agreement with fusion experiments and also with mass variances σ_{AA}^2 . D. Boilley showed that the neck fomation is a key ingredient and that the appearance of fusion hindrance sets some constraints on the fusion barriers.

3.6 Transfer Channels

Assuming that α in Eq. 4 is simply the time *t*, and using the first-Born approximation (i.e, taking $a_k \sim a_0 \delta_{k0}$), the amplitude to excite the channel ϕ_k from an initial channel ϕ_0 is given by $a_k = -i\hbar \int \langle \phi_0 | U | \phi_k \rangle \exp[i(E_k - E_0)t/\hbar]$. The Born approximation can be applied to transfer reactions, as shown by *G. Pollarolo*. The probability to transfer a nucleon in nucleus A from channel α to a nucleon in nucleus



Fig. 7. Interpretation of the measured capture and fusion excitation functions by description of evaporation residue cross sections. (Courtesy of *H. Zhang*).

B in channel β is given by

$$P_{\beta\alpha} \sim \left| -i\hbar \int_{-\infty}^{\infty} dt F_{\beta\alpha}(\mathbf{R}) \exp\left[i\frac{E_{\beta}-E_{\alpha})t}{\hbar} + (\cdots)\right] \right|^2, \quad (7)$$

where **R** is the nucleus-nucleus distance and $F_{\beta\alpha}(\mathbf{R})$ is the from factor given by

$$F_{\beta\alpha}(\mathbf{R}) = \int d^3 r e^{i\mathbf{Q}\cdot\mathbf{r}} \phi_{\beta}(\mathbf{R}+\mathbf{r}) \left(V_1 - \langle U \rangle\right) \phi_{\alpha}(\mathbf{r}), \quad (8)$$

where **Q** is the momentum transfer in the reaction, U is the total (optical) potential, and V_1 is the potential of the nucleon with one of the nuclei. Why not V_2 ? In the literature, using V_1 (V_2) goes by the name "*prior*"("*post*)-*form*. It has been shown in the past that the post and prior forms of breakup and transfer reactions lead to the same result. You should not worry with this. But you should worry with the (\cdots) in Eq. 7. They are often associated with an *Uncontrolled Theoretical Ignorance* (UTI). Dangerous stuff.

In figure 6, shown by *L. Corradi*, one sees the probabilities for multinucleon transfer in ${}^{96}\text{Zr}+{}^{40}\text{Ca}$, as a function of the closest approach distance $D = (Z_1Z_2e^2/2E)$ $[1 + 1/\sin(\theta/2)]$. Transfer is most likely to occur when the nuclei are at their closest point, *D*. The tunneling probability depends exponentially on this distance, $P_{tr}/\sin(\theta/2) \sim \exp(-2\alpha D)$. This approximation arises from Eqs. 7 and 8. If one neglects correlations, two-nucleon transfer probabilities are given in terms one-nucleon transfer probabilities: $P_{2n} = (P_{1n})^2$. For three-nucleon transfer $P_{3n} = P_{1n}P_{2n}$, and so on. These are shown by the straight lines in figure 6. All seems to work well, except that one needs an *enhancement of a factor 3* to get P_{2n} from theory [10]. Mystery! In *Corradi*'s words: "*that is what happens when theorists do not know what to do*". Who am I to disagree?

F. Scarlassara presented ${}^{60}\text{Ni}+{}^{100}\text{Mo}$ fusion data below the barrier. He claims that the experiment is not conclusive with regard to the possible transfer effect on deep sub-barrier fusion. *F. Liang* claims that a large sub-barrier

fusion enhancement has been observed in reactions with 40 Ca. Comparing to the fusion with 48 Ca, the enhancement in 40 Ca can be attributed to neutron transfer. Multinucleon transfer reactions have also been investigated in 40 Ar+ 208 Pb, reported by *S. Szilner*.

M. Evers showed data on the reactions ²⁰⁸Pb(¹⁶O,¹⁴O) ²¹⁰Po, ²⁰⁸Pb(¹⁶O,¹²O)²¹²Po and ²⁰⁸Pb(¹⁶O,¹⁵O)²⁰⁹Bi. He also concludes that multi-nucleon transfer processes already play an important role at energies well below the fusion barrier. *C. Beck* also reported on the need of nucleon transfer to explain sub-barrier fusion of ³²S+⁹⁶Zr and ⁴⁰Ca+ ^{90,96}Zr. *I. Martel* also discussed effects of neutron transfer on fusion of light halo nuclei at Coulomb barrier energies.

3.7 Incomplete Fusion, Fission, Evaporation

The cross section for fusion evaporation can be written as

$$\sigma_{EV}(E) = \sigma_{cap}(E)P_{CN}(E)W_{sur}(E), \qquad (9)$$

where σ_{cap} is the capture cross section, P_{CN} is the probability of compound nucleus formation and W_{sur} is the probability of survival through quasi-fusion processes. Processes such as fusion-fission take the order of 10^{-18} s to happen, whereas quasi-fission takes only 10^{-21} s. Detectors do not know that, unless they are pretty fast. Humans intervene. The evaporation residue (ER) probabilities are usually calculated by means of the Hauser-Feshbach theory incorporated in popular free numerical codes such as HIVAP, PACE or TALYS.

P.P. Singh reported an unexpected increase of incomplete fusion (ICF) for energies above V_B . *D.J Hinde* discussed an improved modeling of ICF. *A. Wakhle* presented calculations which show that shell effects around ²⁰⁸Pb strongly affect reaction dynamics in ICF reactions.

H. Zhang presented data analysis for the competition between fusion-fission and quasi-fission in the 32 S+ 184 W reaction. Figure 7 shows his interpretation of the measured capture and fusion excitation functions by description of evaporation residue cross sections.

J. Khuyagbaatar reported measurements of fission crosssections of ³⁴S and ³⁶S induced reactions with ^{204,206,208}Pb targets. A larger enhancement of the capture cross-sections below the interaction barriers was observed for ³⁴S compared to ³⁶S. The experimental results well described except for ²⁰⁴Pb (N=122) where the experimental fission crosssections indicates some enhancement due to higher order channel couplings. A significantly lower experimental ER cross-sections for ³⁴S compared to calculations show a hint at an additional effect which hinders fusion in the ³⁴S induced reaction.

Lukyanov discussed the 2n-evaporation channel in the fusion of ${}^{4.6}$ He+ 208,206 Pb reactions, leading to the same compound nucleus. The excitation functions for the 2n evaporation channels were obtained at energies below the sub-Coulomb barrier region. A large value of the fusion cross section was observed in the case of the reaction induced by the weakly bound 6 He projectile due to multi-neutron transfers.



Fig. 8. Reduced cross sections for the fusion of halo, normal/weakly bound, and strongly bound nuclei. (Courtesy of *J. Kolata*).

N. Rowley claims that the creation of evaporation residues is a very complicated three stage process. The frequently used Eq. 9 is at best schematic, with *P* and *W* ill-defined averages. He proposed a new relation where all quantities are well-defined, and then he thaught us how to interpret it theoretically. He demonstrated this with respect to the many systems leading to ¹²⁰Th for which many good data exist. All this time *we have been fooled*, folks! At least now we know it.

D. Pierroutsakou presented the results of a systematic study of the excitation of dynamical dipole modes as a function of the beam energy in fusion reactions leading to the 132 Ce compound nucleus. There is evidence that the prompt dipole radiation is confined at the first moments of the reaction. *K. Nishio* reported an investigation of fission properties and evaporation residue measurement in reactions using 238 U target nucleus. *K. Masurek* discussed the influence of the potential energy landscape on the fission dynamics.

D. Mancusi discussed the constraining of statisticalmodel parameters using fusion and spallation reactions. *G. Ademard* reported studies on the decay of excited nuclei produced in the 78,82 Kr+ 40 Ca reactions at 5.5 MeV/nucleon.

4 Special Topics

4.1 Rare Isotopes

P. Gomes introduced a Universal Fusion Function (UFF) to investigate the role of breakup dynamical effects on fusion of neutron halo ⁶He weakly bound systems. The idea is that one divides and multiplies the calculated fusion cross sections by factors which account for the major physics behind fusion. Then the deviations from the expected UFF are a hint of coupled channel effects (unknown physics, I told you.). By comparing the UFF with data on fusion of ⁶He and ¹¹Be on numerous targets, he concludes that there is a suppression above the barrier and an enhancement below the barrier. The UFF idea reminds me of ef-



Fig. 9. Fusion cross sections of ^{4,6,8}He with ¹⁹⁷Au.The inset is the reduced (scaled) cross sections. (Courtesy of *A. Lemasson*)

forts to find a *grand unified theory of everything* in particle physics. Ambitious, specially for nuclear physicists.

M. Alcorta and *E. Rehm* presented new measurements of fusion-fission cross sections for the systems 13,14,15 C + 232 Th. They conclude that fusion of 14 C+ 232 Th is similar to that of 12,13 C+ 232 Th and that fusion of 15 C+ 232 Th shows a fusion enhancement by a factor of 5-6 at $E/V_B \sim 0.85$. *A. Di Pietro* showed a damping of elastic cross-section for the reaction induced by the 11 Be nucleus when compared with both 9 Be ($S_n = 1.67$ MeV) and 10 Be ($S_n = 6.8$ MeV).

E. F. Aguilera and *J. Kolata* presented new data on evaporation protons from ${}^{8}B+{}^{58}Ni$ at 8 energies. Perhaps the most impressive result from this group is shown in figure 8. One sees the reduced (scaled by geometry) cross sections for the fusion of halo, normal/weakly bound, and strongly bound nuclei. A clear tendency is seen of fusion enhancement with decreasing binding energy.

V. Guimarães discussed an optical model analyses with double-folding São Paulo Potential for 7,8,9 Be+ 12 C elastic scattering. *M. Mazzocco* presented data on quasi-elastic angular distributions for 17 F. The collected data were analyzed within the framework of the optical model with the coupled-channels to extract the reaction cross sections and to investigate the relevance of direct reaction mechanisms. Only a very small influence of the 17 F low binding energy on the reaction dynamics was found.

W. Loveland claims that ⁹Li fusion excitation functions show sub-barrier fusion enhancement which are not easily accounted for by current models of fusion. He also mentioned that to understand this better one would need to measure the fusion of ¹¹Li+²⁰⁸Pb, the "*holy grail*" of fusion reactions. This reminds me of my preferred Monty Python quote: "*we are the knights who say ni*".

G. Potel presented a calculation of nucleon-pair transfer in reactions with neutron-rich nuclei using concepts of the BCS theory. He finds that the absolute cross section associated with the first excited state of ⁹Li in the $p(^{11}\text{Li}, ^{9}\text{Li}*(1/2^{-}; 2:69\text{MeV}))$ t reaction is a *direct evidence* of phonon mediated pairing in nuclei. His method is an

extension of Eqs. 7 and 8, with $P_{\beta\alpha}$ now including four nucleon wavefunctions for simultaneous two-neutron transfer. He also includes sequential two-neutron transfer. In this case a nucleon propagator for the intermediate state is included.

L.V. Grigorenko discussed new theoretical advances in studies of two-proton radioactivity and three-body decays. The lifetime and decay energy systematics for several known and prospective true 2p emitters were calculated.

Sh. A. Kalandarov reported the production of the doubly magic nucleus 100 Sn in 72,74,76 Kr $^{+40}$ Ca, 72,74,76 Kr $^{+40}$ Ar and 72,74,76 Kr $^{+32}$ S reactions at 4-6 MeV/nucleon. N. Madhavan reported a new gas-filled separator to be built at New Delhi. The relevance of breakup of 6,7 Li in fusion reactions was discussed by D. Luong. A. Drouart reported a new toy: the S^3 - Super Separator Spectrometer - at GANIL.

A. Lemasson showed new data on fusion of ^{4,6,8}He. He reported an unexpected similar behavior of the cross sections for ⁶He and ⁸He [12]: the additional two neutrons do not modify the tunneling probability (see figure 9). These results might be a showcase for the general problem of *tunneling of composite objects* [13]: in loosely-bound systems, tunneling of clusters might occur with different time-scales. Similar study was presented by *Y. Penionzhkevich*.

4.2 Clusters

J. Maruhn discussed the new advances in α -cluster formation in nuclei based on a time-dependent Hartree-Fock (TDHF) method. Results showing α -chain states in ^{12,16,20}C were presented. Also, a chain state in ¹⁶O provides rotational stabilization. Maruhn also announced the discovery of "numerical tunneling". This is shown in figure 10. A convergence indicator is used to assess if the ground state of the hamiltonian h is reached,

$$\varDelta h = \frac{1}{A} \sum_{k} \sqrt{\langle \phi_k | \hat{h}^2 | \phi_k \rangle - \langle \phi_k | \hat{h} | \phi_k \rangle^2}.$$

An excited quasi-stable state appears as an apparently converged configuration for 1000's of iterations. But then, suddenly, unexpectedly, and also puzzlingly, there is convergence path to the ground state via triaxial shapes. This only happens if you allow the computer code to run way beyond what you (wisely) would ask it to do. Isn't that worth an international prize? At least the *Ig nobel prize*, please.

M. Ito reported studies of light neutron-excess systems from bound to continuum states. His method is based on molecular states in nuclei. In particular, he calculated highly excited states of Be isotopes and in ^xHe+^yHe reactions. He observed cluster structures in light 4N nuclei and in α cluster nuclei such as ⁸Be= 2α , ¹²C= 3α , ¹⁶O= α +¹²C. He also showed the monopole response of ¹²Be and its ratio to single-particle response in the continuum.

4.3 Nuclear Astrophysics

A. Guglielmetti presented recent results on (p,γ) and (α, γ) fusion reactions at the LUNA facility. In particular, she



Fig. 10. The discovery of "numerical tunneling". (Courtesy of *J. Maruhn*).

presented the new S-factor for ³He+⁴He reaction, $S_{34} = 0.567 \pm 0.018 \pm 0.004$ keV b. The reduced uncertainty due to S_{34} on neutrino flux implies a reduction $\Phi_{^8B} = 7.5\% \rightarrow 4.3\%$ and $\Phi_{^7Be} = 8\% \rightarrow 4.5\%$.

F. de Oliveira Santos presented new results for ¹⁸F(p, α) ¹⁵O, H(¹⁷Ne,p)¹⁷Ne, H(¹⁴O,p)¹⁴O. *R.G. Pizzone* discussed the "*Trojan Horse Method*" (THM) used to determine the cross section for the ⁶Li(d, α)⁴He reaction. The excitation function obtained from direct data of the ⁶Li(d, α)⁴He and ⁷Li(p, α)⁴He is well reproduced by THM below and above the Coulomb barrier in both cases, which attests theTHM particle invariance, or *pole invariance*.

B. Jurado presented new results on surrogate reactions, e.g., (n,f) obtained from transfer reactions. A major challenge for this method is to show that the population of states via a "*surrogate reaction*" is the same as that for capture of a free neutron. In the case of independence on the population of angular momentum states J^{π} , the reaction can be described by the Ewing-Weisskopf theory (EWT). Hauser-Feshbach theory is the same as EWT with proper account of angular momentum. A successful case is shown in figure 13. Excellent agreement of EWT calculations at low energies for this case, shows that the fission cross sections are not sensitive to differences J^{π} distributions [14]. Unfortunately, this seems to be more an exception that the rule.

A. Goasduff reported measurements of ${}^{12}C+{}^{16}O$ subbarrier radiative capture cross sections. K. Czerski and J. Kasagi presented results on enhanced electron screening in nuclear reactions Their data show a much enhanced fusion cross section within liquids and metals, which cannot be explained by theory [15]. This unavoidably reminds me of the cold fusion saga. Let us hope that it really works. In this way we could avoid paying the bill for ITER and other machines. It would also save a lot of space in France.

4.4 Superheavy Elements

In the 1960's a famous Russian professor was invited for a conference in France. "Professor, this was very nice", said the conference chairman at the end of his talk, "but I did not understand why you talked for 5 minutes and sat down for another 5 minutes, repeatedly during your seminar", continued the chairman. "I am very sorry", replied



Fig. 11. New S-factor for ³He+⁴He reaction from the LUNA collaboration. (Courtesy of *A. Guglielmetti*).

the Professor, "but I was told by my comrades in Russia that the French are very slow thinkers. Thus I was giving you time to understand what I said". If you participated in this conference, you know that I am not joking.

J. Hamilton reported on the discovery of the new superheavy element (SHE) with Z=117. This was a mark achievement in this field, and was only possible with the finding that one needed ²⁴⁹Bk to produce the fusion of ⁴⁸Ca and ²⁴⁹Bk, followed by 3n evaporation [16]. Berkelium was produced and bought from the Oak Ridge National Lab at a very salty price and shipped to Dubna/Russia where the superheavy science was done. It is a clear realization that the US has turned from a major science achiever to an *exporter of raw material*, a real B-republic (B is for Berkelium, not Banana).

K. Morita presented the latest efforts at RIKEN on (a) the reaction 209 Bi(70 Zn,n) 278 113, with a cross-section of 18 + 25 - 13 fb, (b) new spectroscopic data on 266 Bh, 262 Db with further confirmation of 278 113, and 265 Sg^{*a*/*b*}, 261 Rf^{*a*/*b*} with further confirmation of 277 Cn, and on 264 Hs, 263 Hs. A dedicated community work.

A. Karpov discussed ternary quasi-fission of giant nuclear systems. True ternary fission is impossible for actinides (insufficient mass). Superheavy nuclei have a real chance to split onto tin + something + tin. Giant nuclear molecules may decay onto lead + something + lead.

A. A. Voinov discussed the reaction 226 Ra+ 48 Ca= 269 - 271 Hs+3-5n. Six decay chains of 270 Hs were observed at 233 MeV beam energy. A cross section $\sigma_{4n} = 8.3$ pb was measured to be lower than predicted. No decay chains of $^{269-271}$ Hs isotopes were observed at two other bombarding energies of 228.5 MeV and 240.5 MeV. The upper cross section limits are $\sigma_{3n} < 4.2$ pb and $\sigma_{5n} < 5.0$ pb for the low and high 48 Ca beam energy, respectively

M. Itkis taught us how to measure reactions with ⁴⁸Ca. ⁴⁸Ca is a *best kept secret* by the Russians. With ⁴⁸Ca the newest elements were found. Why did it take so long to realize that ⁴⁸Ca was THE nucleus? The double-magic nucleus ⁴⁸Ca allows one to obtain the low excitation energy of compound nucleus ($E^* \sim 30 - 36$ MeV) at the Coulomb barrier. The neutron excess leads to $N_{CN} = 170 - 180$ in the reaction with actinide targets in contrast to cold fusion reactions, where $N_{CN} \sim 150 - 160$. The heaviest element, which can be obtained with the reactions with ⁴⁸Ca



Fig. 12. Fission cross sections following neutron capture on 241 Am obtained from the surrogate method. The data is well explained without need for accounting for J^{π} distributions. (Courtesy of *B. Jurado*).

projectiles, is the 118 nucleus. *Itkis* claims that a possible alternative pathway for SHE synthesis is represented by the complete fusion of actinide nuclei with heavier projectiles such as ⁵⁸Fe or ⁶⁴Ni leading to the formation of CN with Z = 118 - 124 and N = 178 - 188.

P. Armsbruster claims that it is hard to understand the production cross sections for reactions induced by beams beyond ⁴⁸Ca. In fact, it seems to be hard to understand the unexpectedly high cross sections with ⁴⁸Ca. One needs to carry out experiments to determine the atomic numbers of the elements Z = 114-118, either by chemistry or by characteristic *K* and *L X*-ray energies. Armbruster also mentioned that fission of oblate nuclei has never been observed. Their fission probabilities should be measured. By the way, Happy 80th Birthday, Peter! We hope that you continue to help us understand the nature of fusion and fission for a long time.

Christoph E. Düllmann discussed the TASCA research program where element 114 was identified with high cross sections (10 pb) and high efficiency (60%), what open up new avenues for other experiments. Next experiments will focus on direct Z determination of ${}^{48}\text{Ca}{+}^{243}\text{Am}$ products and the search for element 120.

Finally, V. Zagrebaev taught us that the time-dependent Schrödinger equation shows us (only if you ask it right) that at low-energy collisions nucleons do not "jump" from one nucleus to another. The wave functions of valence nucleons follow the *two-center molecular states* spreading over both nuclei. Two-Center Shell Model + Adiabatic Potential Energy Surface + Transport (Langevin type) Equations of Motion are appropriate for description of low-energy multi-nucleon transfer [17]. In the end, he presented new ideas towards heavier elements: (a) produce SHE with pulsed nuclear reactors, (b) produce SHE in multiple (rather soft!) *nuclear explosions* [18]. Wow! I like the ideas, even the last one. But I only hope that they perform this experiment within the borders of the Russian Federation.



Fig. 13. Fusion cross sections leading to the formation of superheavy elements. (Courtesy of *Christoph E. Düllmann*).

The meeting was a huge success because of the dedicated work of the organizers Navin Alahari (chair), Héloise Goutte, Denis Lacroix, Christine Lemaitre, Maurycy Rejmund and Christelle Schmitt. We are thankful for their community service and for the usual great French hospitality (and for the delicious food, of course).

The next FUSION conference was chosen by the International Advisory Committee to be held in *New Delhi*, *India*, 2014. I can't wait.

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