

Description

Exam #1: Please work as many problems as possible showing ALL work! Even if you have to write your thought process in English, please do NOT simply state the answers.

1. Question Details

SPreCalc6 1.1.005.MI. [2684203]

List the elements of the given set that are natural numbers, integers, rational numbers, and irrational numbers. (Enter your answers as comma-separated lists.)

$$\left\{ 0, -15, 20, 25, 1, \frac{22}{7}, 0.538, \sqrt{8}, \pi, -\frac{1}{3}, \sqrt[3]{2} \right\}$$

(a) natural numbers

20, 25, 1

(b) integers

0, -15, 20, 25, 1

(c) rational numbers

0, -15, 20, 25, 1, $\frac{22}{7}$, 0.538, $-\frac{1}{3}$

(d) irrational numbers

$2\sqrt{2}, \pi, \sqrt[3]{2}$

2. Question Details

SPreCalc6 1.1.044.MI. [1615695]

Find the indicated set if given the following.

$$A = \{x|x \geq -8\} \quad B = \{x|x < 5\} \quad C = \{x|-1 < x \leq 6\}$$

(a) $A \cap C$

- $\{ x | -8 \leq x < 5 \}$
- $\{ x | -8 \leq x \leq 5 \}$
- $\{ x | -1 < x \leq 6 \}$
- $\{ x | -1 \leq x \leq 6 \}$
- none of these

(b) $A \cap B$

- $\{ x | -8 \leq x < 5 \}$
- $\{ x | -8 \leq x \leq 5 \}$
- $\{ x | -1 < x \leq 6 \}$
- $\{ x | -1 \leq x \leq 6 \}$
- none of these

Simplify the expression and eliminate any negative exponent(s).

(a) $\frac{6a^5b^{-3}}{2a^{-6}b^9}$

$$\frac{3a^{11}}{b^{12}}$$

(b) $\left(\frac{y}{2x^{-2}}\right)^{-3}$

$$\frac{8}{x^6y^3}$$

Factor the trinomial.

$$3x^2 - 25x + 42$$

$$(x - 6)(3x - 7)$$

Factor the trinomial.

$$(2x + 3)^2 + 6(2x + 3) + 8$$

$$(2x + 5)(2x + 7)$$

Use a Special Factoring Formula to factor the expression.

$$(x + 5)^2 - 16$$

$$(x + 1)(x + 9)$$

Factor the expression by grouping terms.

$$2x^3 + 7x^2 - 6x - 21$$

$$(2x + 7)(x^2 - 3)$$

Find the domain of the expression.

$$\frac{1}{\sqrt{x - 1}}$$

- $x \geq 1$
- $x > 1$
- $x < 1$
- $x \leq 0$
- all real numbers

Perform the addition or subtraction and simplify. (Give your answer in factored form.)

$$\frac{1}{x+9} + \frac{5}{x-8}$$

$$\frac{6x+37}{(x+9)(x-8)}$$

Solve the equation by factoring.

$$6x(x-1) = 25 - 11x$$

$$x = \boxed{} \quad \boxed{-5/2} \text{ (smaller value)}$$

$$x = \boxed{} \quad \boxed{5/3} \text{ (larger value)}$$

Evaluate the function at the indicated values. (If an answer is undefined, enter UNDEFINED.)

$$f(x) = x^2 - 6$$

$$f(-3) = \boxed{3}$$

$$f(3) = \boxed{3}$$

$$f(0) = \boxed{-6}$$

$$f\left(\frac{1}{2}\right) = \boxed{-5.75}$$

$$f(10) = \boxed{94}$$

Evaluate the function at the indicated values. (If an answer is undefined, enter UNDEFINED.)

$$f(x) = 6x^2 + 2x - 12$$

$$f(0) = \boxed{-12}$$

$$f(2) = \boxed{16}$$

$$f(-2) = \boxed{8}$$






$$f(\sqrt{2}) = \boxed{2\sqrt{2}}$$

$$f(x+1) = \boxed{6x^2 + 14x - 4}$$

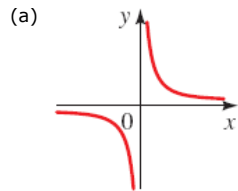
$$f(-x) = \boxed{6x^2 - 2x - 12}$$


Evaluate the piecewise defined function at the indicated values.

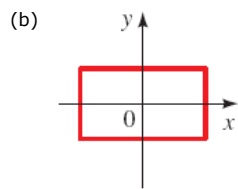
$$f(x) = \begin{cases} x^2 & \text{if } x < 0 \\ x + 3 & \text{if } x \geq 0 \end{cases}$$


$f(-4) =$  16
 $f(-3) =$  9
 $f(0) =$  3
 $f(3) =$  6
 $f(4) =$  7

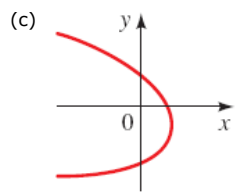
Use the Vertical Line Test to determine whether the curve is the graph of a function of x .




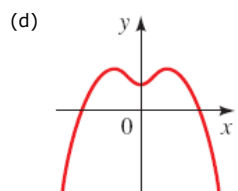
-  is a function
- is not a function




- is a function
-  is not a function

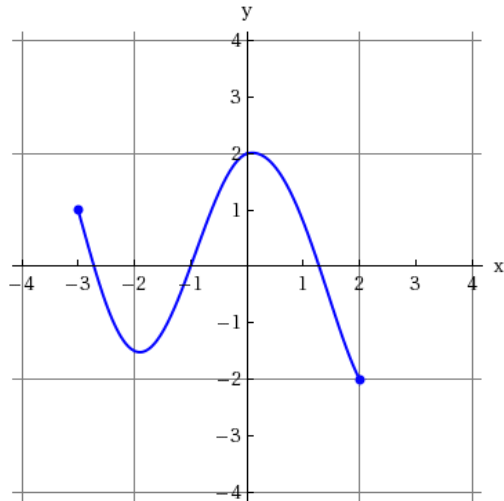


- is a function
-  is not a function




-  is a function
- is not a function

Consider the following graph.



Use the Vertical Line Test to determine whether the curve is the graph of a function of x .

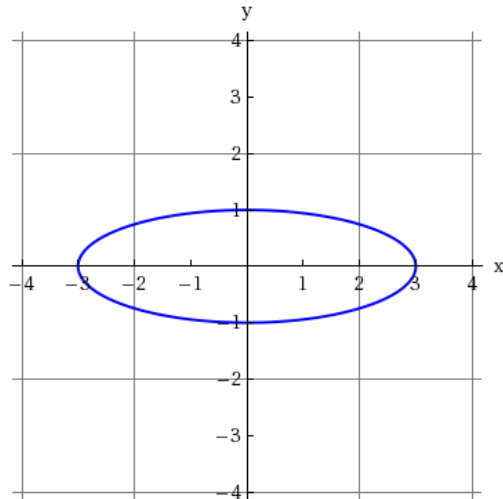
-  Yes, the curve is a function of x .
- No, the curve is not a function of x .

If the curve is a function, state the domain and range. (Enter your answers using interval notation. If the curve is not a function enter NONE.)

domain

range

Consider the following graph.



Use the Vertical Line Test to determine whether the curve is the graph of a function of x .

- Yes, the curve is a function of x .
- No, the curve is not a function of x .

If the curve is a function, state the domain and range. (Enter your answers using interval notation. If the curve is not a function enter NONE.)

domain

NONE

range

NONE

Determine whether the equation defines y as a function of x . (See Example 9.)

$$x^2 + (y - 3)^2 = 8$$

- is a function
- is not a function

Determine whether the equation defines y as a function of x . (See Example 9.)

$$x^2y + y = 2$$

- is a function
- is not a function

Fill in the blank with the appropriate axis (x -axis or y -axis).

(a) The graph of $y = -f(x)$ is obtained from the graph of $y = f(x)$ by reflecting in the ---Select--- .

(b) The graph of $y = f(-x)$ is obtained from the graph of $y = f(x)$ by reflecting in the ---Select--- .

Suppose the graph of f is given. Describe how the graph of each function can be obtained from the graph of f .

(a) $y = 7f(x + 6) - 2$

- shift right 6 units, stretch horizontally by a factor of 7, then shift up 2 units
- shift right 6 units, stretch horizontally by a factor of 7, then shift down 2 units
- shift left 6 units, stretch vertically by a factor of 7, then shift up 2 units
- shift left 6 units, stretch horizontally by a factor of 7, then shift down 2 units
- shift left 6 units, stretch vertically by a factor of 7, then shift down 2 units

(b) $y = 7f(x - 6) + 2$

- shift right 6 units, stretch vertically by a factor of 7, then shift up 2 units
- shift left 6 units, stretch horizontally by a factor of 7, then shift up 2 units
- shift right 6 units, stretch horizontally by a factor of 7, then shift up 2 units
- shift right 6 units, stretch vertically by a factor of 7, then shift down 2 units
- shift left 6 units, stretch horizontally by a factor of 7, then shift down 2 units

True or false?

(a) If f has an inverse, then f^{-1} is the same as $\frac{1}{f(x)}$.

- true
- false

(b) If f has an inverse, then $f^{-1}(f(x)) = x$.

- true
- false

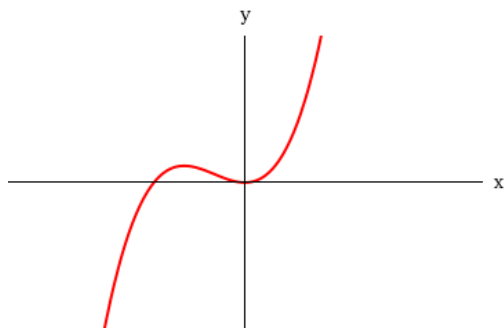
A function f is given, and the indicated transformations are applied to its graph (in the given order). Write the equation for the final transformed graph.

$f(x) = \sqrt[4]{x}$; reflect in the y -axis and shift upward 2 units

$y =$

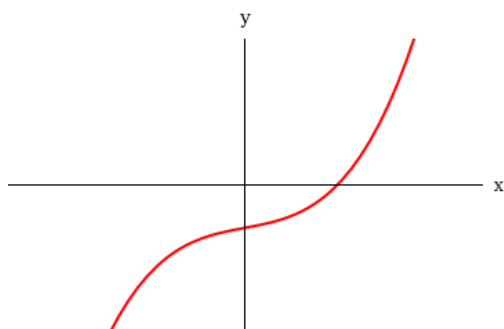
The graph of a function f is given. Determine whether f is one-to-one.

- is one-to-one
- is not one-to-one



The graph of a function f is given. Determine whether f is one-to-one.

- is one-to-one
- is not one-to-one



Determine whether the function is one-to-one.

$$f(x) = 3x - 7$$

- is one-to-one
- is not one-to-one

Question

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Description

This is Exam #2. Please work all the problems, showing ALL necessary work.

1. Question Details

SPreCalc6 5.1.009. [2684190]

Find the missing coordinate of P , using the fact that P lies on the unit circle in the given quadrant.

Coordinates	Quadrant
$P\left(-\frac{4}{5}, \frac{3}{5}\right)$	III

2. Question Details

SPreCalc6 5.1.011. [2684220]

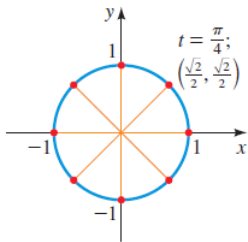
Find the missing coordinate of P , using the fact that P lies on the unit circle in the given quadrant.

Coordinates	Quadrant
$P\left(-\frac{2\sqrt{6}}{5}, \frac{1}{5}\right)$	II

3. Question Details

SPreCalc6 5.1.021. [1713018]

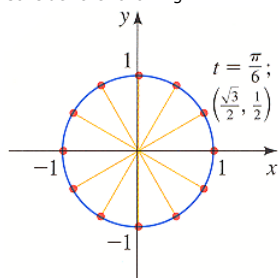
Consider the following.



Find t and the terminal point determined by t for each point in the figure, where t is increasing in increments of $\pi/4$.

t	Terminal Point
0	$(1, 0)$
$\frac{\pi}{4}$	$\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$
$\frac{\pi}{2}$	$(0, 1)$
$\frac{3\pi}{4}$	$\left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$
π	$(-1, 0)$
$\frac{5\pi}{4}$	$\left(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$
$\frac{3\pi}{2}$	$(0, -1)$
$\frac{7\pi}{4}$	$\left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$
2π	$(1, 0)$

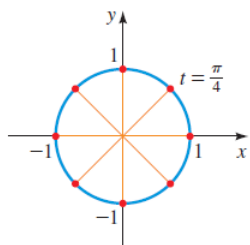
Consider the following.



Find t and the terminal point determined by t for each point in the figure, where t is increasing in increments of $\pi/6$.

t	Terminal Point
0	(<input type="text" value="1"/> , <input type="text" value="0"/>)
$\frac{\pi}{6}$	(<input type="text" value="sqrt(3)/2"/> , <input type="text" value="1/2"/>)
<input type="text" value="pi/3"/>	(<input type="text" value="1/2"/> , <input type="text" value="sqrt(3)/2"/>)
<input type="text" value="pi/2"/>	(<input type="text" value="0"/> , <input type="text" value="1"/>)
<input type="text" value="2pi/3"/>	(<input type="text" value="-1/2"/> , <input type="text" value="sqrt(3)/2"/>)
<input type="text" value="5pi/6"/>	(<input type="text" value="-sqrt(3)/2"/> , <input type="text" value="1/2"/>)
<input type="text" value="pi"/>	(<input type="text" value="-1"/> , <input type="text" value="0"/>)
<input type="text" value="7pi/6"/>	(<input type="text" value="-sqrt(3)/2"/> , <input type="text" value="-1/2"/>)
<input type="text" value="4pi/3"/>	(<input type="text" value="-1/2"/> , <input type="text" value="-sqrt(3)/2"/>)
<input type="text" value="3pi/2"/>	(<input type="text" value="0"/> , <input type="text" value="-1"/>)
<input type="text" value="5pi/3"/>	(<input type="text" value="1/2"/> , <input type="text" value="-sqrt(3)/2"/>)
<input type="text" value="11pi/6"/>	(<input type="text" value="sqrt(3)/2"/> , <input type="text" value="-1/2"/>)
2π	(<input type="text" value="1"/> , <input type="text" value="0"/>)

Find $\sin t$ and $\cos t$ for the values of t whose terminal points are shown on the unit circle in the figure. t increases in increments of $\pi/4$.



t	$\sin t$	$\cos t$
0	0	1
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$
$\frac{\pi}{2}$	1	0
$\frac{3\pi}{4}$	$\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$
π	0	-1
$\frac{5\pi}{4}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$
$\frac{3\pi}{2}$	-1	0
$\frac{7\pi}{4}$	$-\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$

Find the exact value of the trigonometric function at the given real number.

(a) $\sin \frac{8\pi}{3}$

$$\frac{\sqrt{3}}{2}$$

(b) $\csc \frac{8\pi}{3}$

$$\frac{2\sqrt{3}}{3}$$

(c) $\cot \frac{8\pi}{3}$

$$-\frac{\sqrt{3}}{3}$$

Find the exact value of the trigonometric function at the given real number.

(a) $\sec \frac{10\pi}{3}$

$$-2$$

(b) $\csc \frac{10\pi}{3}$

$$-\frac{2\sqrt{3}}{3}$$

(c) $\sec\left(-\frac{\pi}{6}\right)$

$$\frac{2\sqrt{3}}{3}$$

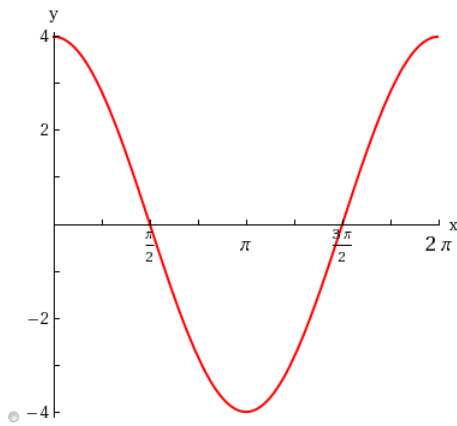
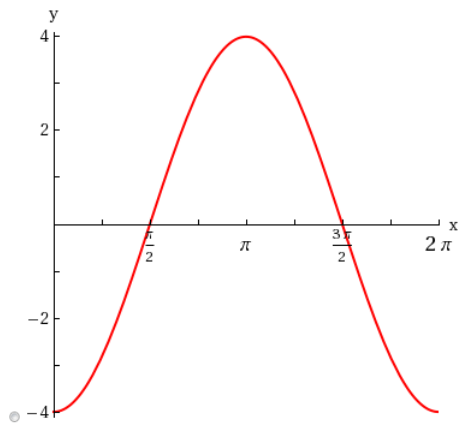
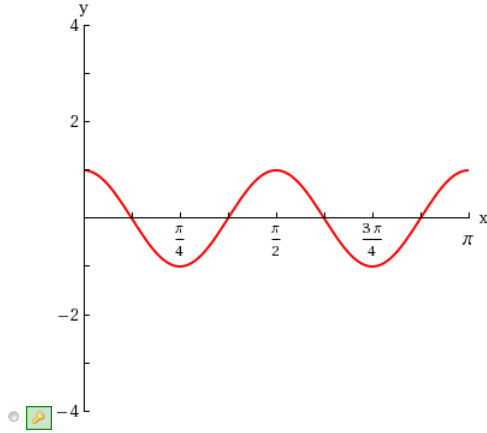
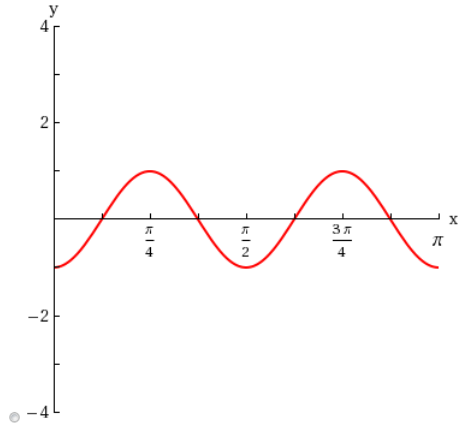
Find the amplitude and period of the function.

$$y = \cos 4x$$

amplitude


period

Sketch the graph of the function.



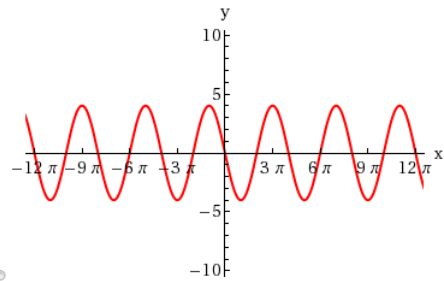
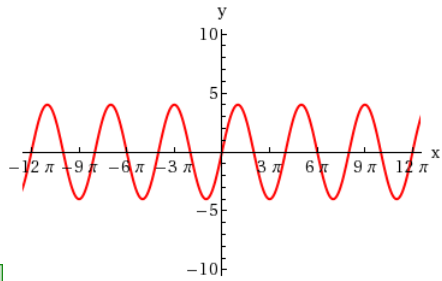
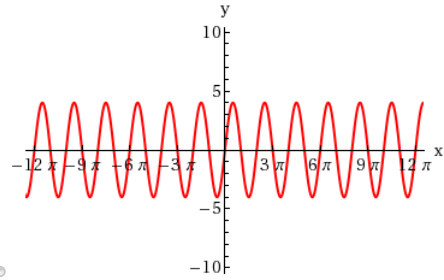
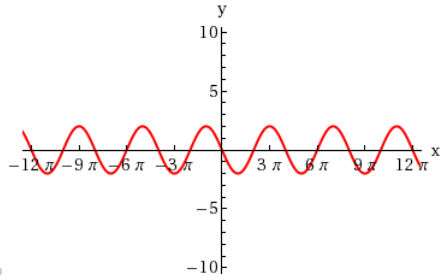
Find the amplitude and period of the function.

$$y = 4 \sin \frac{1}{2}x$$

amplitude 

period 

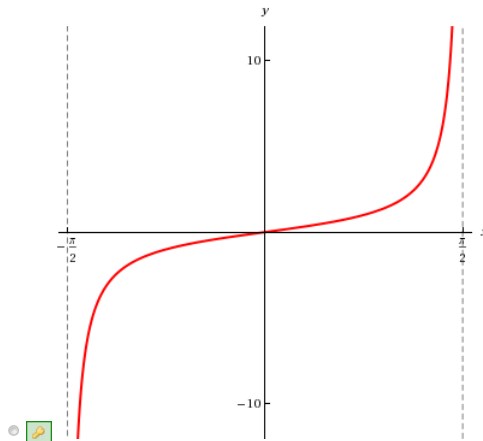
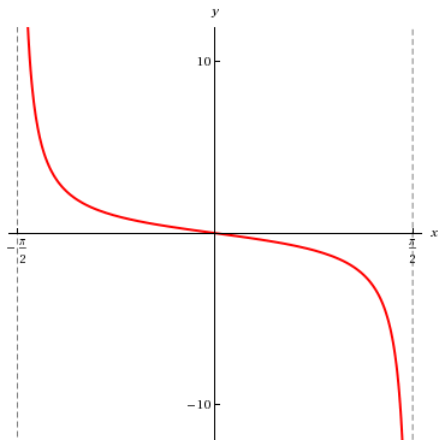
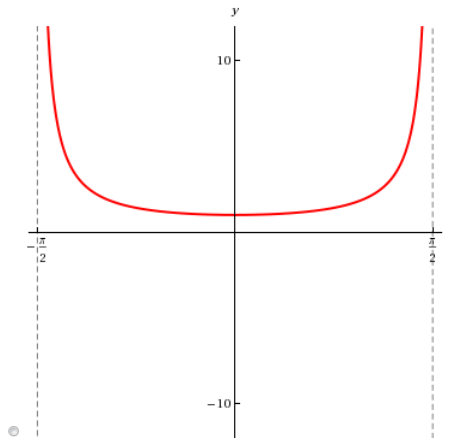
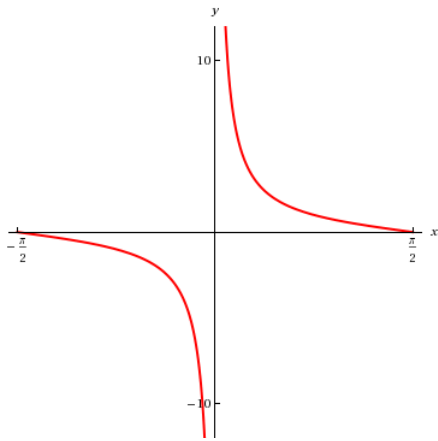
Sketch the graph of the function.



The trigonometric function $y = \tan x$ has period π and the following asymptotes.

- $x = 2n\pi$ (n is an integer)
- $x = \frac{\pi}{2} + 2n\pi$ (n is an integer)
- $x = n\pi$ (n is an integer)
- $x = \frac{\pi}{2} + n\pi$ (n is an integer)
- $x = \frac{3\pi}{2} + 2n\pi$ (n is an integer)

Sketch a graph of this function on the interval $(-\pi/2, \pi/2)$.



Find the degree measure of the angle with the given radian measure.

$$\frac{\pi}{6}$$

 30°

The measure of an angle in standard position is given. Find two positive angles and two negative angles that are coterminal with the given angle. (Enter your answers as a comma-separated list.)

135°

 °

13. Question Details

SPreCalc6 6.1.030. [1776286]

The measure of an angle in standard position is given. Find two positive angles and two negative angles that are coterminal with the given angle. (Enter your answers as a comma-separated list.)

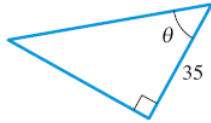
$$\frac{5\pi}{6}$$

$$-\frac{19\pi}{6}, -\frac{7\pi}{6}, \frac{17\pi}{6}, \frac{29\pi}{6} \text{ rad}$$

14. Question Details

SPreCalc6 6.2.033. [1762584]

Solve the right triangle. (Assume $\theta = 53^\circ$.)



Find the length of the side opposite to the given angle. (Round your answer to two decimal places.)

 46.45

Find the length of the hypotenuse. (Round your answer to two decimal places.)

 58.16

Find the other acute angle.

 37°

15. Question Details

SPreCalc6 6.3.036.MI. [2678450]

Find the quadrant in which θ lies from the information given.

$$\tan \theta < 0 \text{ and } \sin \theta > 0$$

- I
- II
- III
- IV

16. Question Details

SPreCalc6 6.3.046. [2708293]

Find the values of the trigonometric functions of θ from the information given.

$$\cos \theta = -\frac{3}{5}, \theta \text{ in Quadrant III}$$

$$\sin \theta = -\frac{4}{5}$$

$$\tan \theta = \frac{4}{3}$$

$$\csc \theta = -\frac{5}{4}$$

$$\sec \theta = -\frac{5}{3}$$

$$\cot \theta = \frac{3}{4}$$

17. Question Details

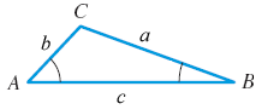
SPreCalc6 6.5.001. [1763555]

In triangle ABC with sides a , b , and c the Law of Sines states that

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

Solve the triangle using the Law of Sines. (Assume $c = 75$, $\angle A = 43^\circ$, and $\angle B = 25^\circ$. Round lengths to two decimal places.)

$a =$
 $b =$
 $\angle C =$ $^\circ$

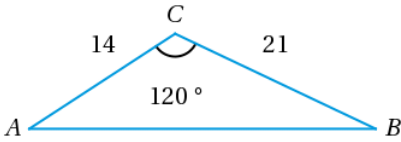


For triangle ABC with sides a , b , and c the Law of Cosines states the following.

$c^2 =$

Solve triangle ABC . (Round the length to three decimal places and the angles to one decimal place.)

$c =$
 $\angle A =$ $^\circ$
 $\angle B =$ $^\circ$



Question

1 2 3 4 5 6 7 8 9 10

Description

This is Exam #3. Please work all the problems, showing ALL necessary work.

1. Question Details

SPreCalc6 7.1.004. [2703858]

Write the trigonometric expression in terms of sine and cosine, and then simplify.

$$\cos t \csc t$$

$$\cot t$$

2. Question Details

SPreCalc6 7.1.017. [2703798]

Simplify the trigonometric expression.

$$\frac{\csc^2 x - 1}{\csc^2 x}$$

$$\cos^2 x$$

3. Question Details

SPreCalc6 7.1.062. [1719017]

Verify the identity.

$$\frac{1 + \sec^2 x}{1 + \tan^2 x} = \cos^2 x + 1$$

Key: Show your work.

4. Question Details

SPreCalc6 7.2.006. [2708244]

Use an Addition or Subtraction Formula to find the exact value of the expression, as demonstrated in [Example 1](#).

$$\cos 165^\circ$$

$$-\frac{\sqrt{6} + \sqrt{2}}{4}$$

5. Question Details

SPreCalc6 7.3.006.MI. [2678458]

Find $\sin 2x$, $\cos 2x$, and $\tan 2x$ from the given information.

$$\csc x = 8, \quad \tan x < 0$$

$$\sin 2x = \boxed{-\frac{3\sqrt{7}}{32}}$$

$$\cos 2x = \boxed{\frac{31}{32}}$$

$$\tan 2x = \boxed{-\frac{3\sqrt{7}}{31}}$$

6. Question Details

SPreCalc6 8.1.031. [2694689]

Find the rectangular coordinates for the point whose polar coordinates are given.

$$(7, 7\pi)$$

$$(x, y) = (\boxed{-7}, \boxed{0})$$

7. Question Details

SPreCalc6 8.1.035-042.501.XP.MI. [1870983]

A point in rectangular coordinates is given. Convert the point to polar coordinates ($r > 0, 0 \leq \theta < 2\pi$).

$$(-7, -7)$$

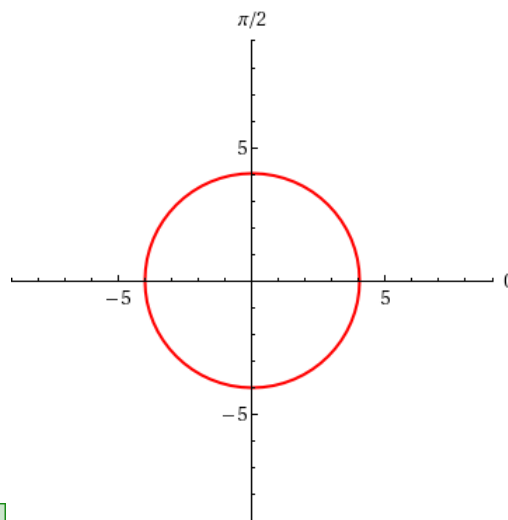
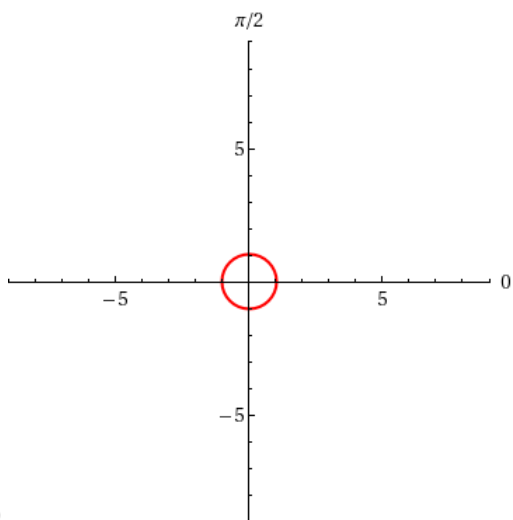
$$(r, \theta) = (\boxed{7\sqrt{2}}, \boxed{\frac{5\pi}{4}})$$

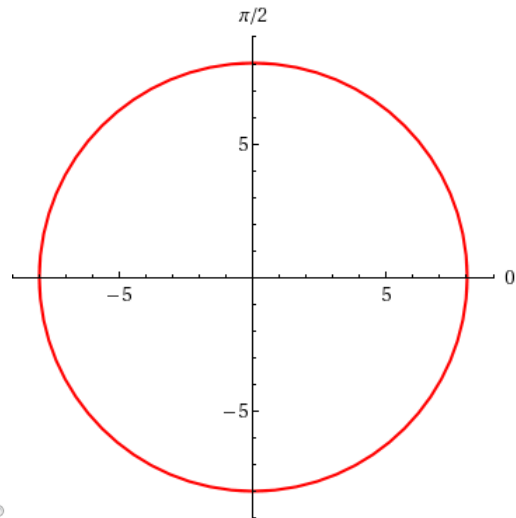
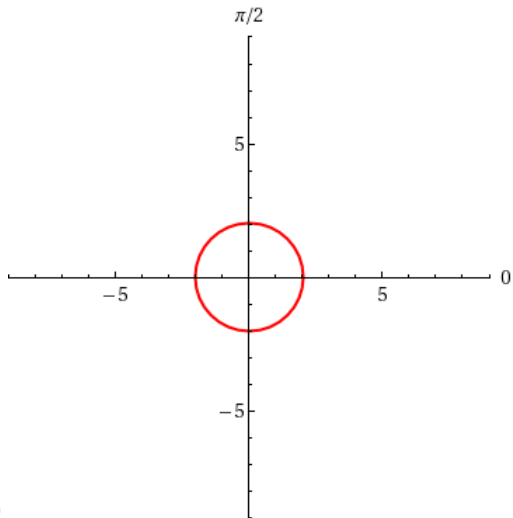
8. Question Details

SPreCalc6 8.2.017. [2706031]

Sketch a graph of the polar equation.

$$r = 4$$





Express the equation in rectangular coordinates. (Use variables x and y .)

9. Question Details

SPreCalc6 8.3.030.MI. [2678942]

Write the complex number in polar form with argument θ between 0 and 2π .

$$3 + 3\sqrt{3}i$$

10. Question Details

SPreCalc6 8.3.069. [1741069]

Find the indicated power using De Moivre's Theorem. (Express your fully simplified answer in the form $a + bi$.)

$$(1 + i)^{12}$$

Assignment Details